UNUSUAL Puzzle
by Nick Ballard

This puzzle, originally entitled "An UNUSUAL Problem," was composed in 1990, when OSPD-1 was the official North American word source. An expansive analysis of that classic version is linked at the end of this article.

The puzzle version described and illustrated below is updated for **NWL-2023** and relatively simplified.

In a 31-round tournament (with no head-to-head playoff), the top four prizes are:

1st = **$10,000** 2nd = **$6000** 3rd = **$3000** 4th = **$1000**

The two leaders have *already finished* the tournament. Here are their final win/losses and point spreads:

Will   24-7, **+2150**
Xavier 24-7, **+2074**

Through no fault of you or your opponent Zoey, your game started after the top games finished, and you already know Will and Xavier's final spreads. It is expected, though not 100% certain, that you or Zoey will end up in third place and the other in fourth place. (You can do no worse, as no one else started the final round better than 21-9.)

You   23-7, **+1000**
Zoey   23-7, **+1000**   (final game pending)

Zoey has just bingoed with 15B OFFERED, to take a massive lead of 479 – 144. You are now on turn, trailing in this final game by **335** points! There are six tiles in the bag. Your rack and unseen pool appear below the diagram. **What is your best play in this unusual situation?**

Scrabble Board

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O
1		C	A	R	I	N	A	S							
2		A	G	I	L	I	T	Y							
3	E	R	O	D	E	D		K							
4	R			A	E			E							
5	E	B	B												
6			I												
7	P	R	A	T				O							
8	A	L	A	T	I	O	N								
9		D	Y	N	A	M	I	C							
10	S			T	I	L	E								
11	I	T		E	N										
12	O	O	S	P	O	R	E	S							
13	I	T		E	U		H								
14	N				E	N									
15	O	F	F	E	R	E	D								

Rack: ? A L S U U U

Unseen: **GGHJMOQVVWWXZ (13)**

Solution

Origin

In the autumn of 1990, while traveling to tournaments, I circulated flyers that featured a puzzle—very similar to the one posed above—as a promotion for my Scrabble newsletter, the title of which spelled out my phone number M-E-D-L-E-Y-S (633-5397). The solution was published in the first issue of *Medleys* (January 1991).

I designed this composition for enjoyment at multiple skill levels. For less experienced players, I wanted the puzzle to seem non-trivial but still easy. The reader could find UnUSUAL and then spot the hook for the blank N above ONCE (possibly needing to check the dictionary for NONCE.) They could then write in to proudly submit their solution and hopefully include with it a $30 subscription check. It worked!

If you play your UnUSUAL bingo (at 6G, for 64 points), your best result is for Zoey's rack (which is *random,* noting that she just bingoed with OFFERED) to be GJQVVWW, which makes your final rack GHMOXZ.

In that case, the best endgame sequence for both sides is shown in the caption of the diagram **below**: Zoey JUG for 22, you MUX (37), and then she repeatedly passes while you play OCARINAS (30), SIZING (155) and SHH (8). You gain 52 from Zoey's rack, and when the smoke clears, despite having outscored her by 324 (!), you still come up short by 11 points: you lose the game 490-501.

UnUSUAL,JUG,MUX+OCARINAS+SIZING+SHH=−11

Heart of the Puzzle

Experts paying attention to the stated problem conditions—realizing that it is a must-win situation—looked beyond UnUSUAL. Examining the 13 unseen tiles, they figured out that if **GHMOVZ** is in the bag and if five or six of these tiles could somehow be combined with the A and/or the blank on their rack, their reward would be to play a maximal-length word on the far left column!

Notwithstanding, the methods by which these savvy experts sought to piece together this fantastic word varied considerably. A few of them recommended passing five tiles, keeping the A and the blank. This is certainly the most direct way. However, either they miscounted the (13) unseen tiles, or they forgot a rule; it is illegal to pass when there are fewer than seven tiles in the bag.

It may seem as if I am overemphasizing the importance of playing a 15-letter word. Some are better than others. In this situation, though, we are potentially looking at a triple-triple-triple bingo that scores up to 1436 points. If you can land it, you will not only turn around the game; you might win the whole tournament!

SOU, EW, SIZING, MU, HAULOUt = –19

SOU, EW, SIZING, XU, HAMULUs = –34

So, SOU me

You can fish for a different bingo by playing 7G SOU. If Zoey has GJQVVWW, she plays 4H EW, and if you draw GZ for SIZING (155), and if Zoey has drawn the M, and X is the last tile in the bag, she plays MU and you go out with HAULOUt (80). You collect 80 from Zoey's rack but still lose by 19. (See **left-hand** diagram **above**.)

A more likely bingo variation: Zoey has any seven of GJQVVWWX, you draw GZ, and O is the last tile in the bag. She plays EW and XU while you play SIZING and HAMULUs and lose by 34. (See **right-hand** diagram **above**.)

However, when followed up properly, SOU aims its sights much higher than a pedestrian bingo. After Zoey plays EW, you should instead empty the bag with J6 ULU (9)! Typical playouts appear in the diagram pair **below**.

Your grand plan culminates in playing the triple-triple-triple OVEREMPHASIZING (abbreviated "OV" in the chart below) for more than 1300 points, like pulling a rabbit out of a hat. If you succeed, more than half the time you will tie for second place, and you even have a chance to acquire *sole* second place. Poor Xavier!

G-rack playout: SOU and SOUL both take 2nd prize   **M-rack playout: SOU ties for 2nd prize, SOUL gets 3rd**

The "G-rack" scenario occurs when Zoey has initially drawn GJQVWWX, plays the W and draws the other G. The full G-rack sequence (starting with your SOU and Zoey's EW) is spelled out in the first row of the chart below. The result is a 1097-point win (highlighted in green), which gloriously vaults you into second place for the $6000 prize. The final position is shown in the **left-hand** diagram **above**.

The "M-rack" scenario occurs in seven related rack-draw possibilities. Zoey starts with seven of the eight tiles GJMQVWWX, plays the W, and draws whichever replacement tile gives her the follow-up rack of GJMQVWX. The full M-rack sequence is spelled out in the chart below. The result is a 1074-point win (highlighted in yellow), which earns you a tie for second place ($4500). The final position is shown in the **right-hand** diagram **above**.

The main reason that you outscore Zoey by more in the left-hand diagram (where Zoey gets both G's) is because playing the blank as a G costs you "only" (2 x 27) + (2 x 3) = 60 points relative to playing an actual G tile. By comparison, in the M-rack situation (on the right), replacing the M with a blank costs you 3 x 27 = 81 points.

For the rest of the rack/draw situations (V, H or O), you get 3rd prize. Based on the tournament situation laid out in the intro, you receive the same amount ($3000) whether you win this final game by 1 point or by 1073 points.

SOU	Rack Pr /1716	Draw	Draw Pr /6	Prob /10296	Sequence		Gain	Game Margin	
					G-rack sequence			SOU	SOUL
GJQVWWX	4	G	1	4	SOU+10, EW-5,　ULU+9, XU-18, OV+1376 + 60		1432	**1097**	1094
GJMQVWW	4	X	1	4	M-rack sequence (as diagrammed above):				
GJMQVWX	8	W	1	8					
GJMQWWX	2	V	2	4	SOU+10, EW-5, ULU+9, MUX-16, OV+1355 +56		1409	**1074**	1071
GJMVWWX	4	Q	1	4					
GJQVWWX	4	M	1	4					
GMQVWWX	4	J	1	4					
JMQVWWX	2	G	2	4					
GJQVVWW	2	X	1	2	V-rack sequence:				
GJQVVWX	4	W	1	4					
GJQVWWX	4	V	1	4	SOU+10, EW-5, ULU+9, XU-18, OV+1324 +64		1384	**1049**	1046
GJVVWWX	2	Q	1	2					
GQVVWWX	2	J	1	2					
JQVVWWX	1	G	2	2					
GJQVWWX	4	H	1	4	H-rack sequence (just twice):		1376	**1041**	1038
HJQVWWX	2	G	2	4	SOU+10, EW-5, ULU+9, XU-18, OV+1316 + 64				
GJQVWWX	4	O	1	4	SOU+10, EW-5, ULU+9, OC-30, pONCE+6, OV+546+72		608	**273**	270
Total winning rack/draw combo = 64/10296					[O-rack sequence is on the row above, one instance]				

The O-sequence is a special case: After playing EW, Zoey draws the O and slips it onto A1 (where you would have put your blank), and your 27-times bingo is diminished to a 9-times non-bingo. Aside from that and a minor twist in the M-sequence (MUX replaces XU), the other sequences are identical. Differences in margin are primarily due to the size of the haircut when the (zero-value) blank substitutes for a real-letter tile.

If Zoey can play two tiles immediately after SOU (e.g., EGG, SOUGH), she pulls two tiles from the bag (when you can afford only one) and you cannot win. Also, if she gets down the 155-point SIZING, her lead is insurmountable even though you can fire back a sizable (five-tile) triple-triple! Thus, no racks listed above contain GG, GH or GZ.

SOUL of the Puzzle

You win the game more often with SOUL (22 rack/draw situations compared to SOU's 17), because if Zoey holds **GH** plus any five of JQVWWX (the five entries in the second chart), she is denied the two-tile reply of SOUGH. Instead, she has to settle for EW, ULU, XU, when you go out with OVEREMPhASIZING and win by 1038.

SOUL (additional)	Rack Pr /1716	Draw	Draw Pr /6	Prob /10296	Sequence	Gain	Game Margin
GHJQVWW	4	X	1	4	H-rack sequence (five more ways): SOUL+11, EW-5, ULU+5, XU-18, OV+1316 + 64	1373	1038
GHJQVWX	8	W	1	8			
GHJQWWX	4	V	2	8			
GHJVWWX	4	Q	1	4			
GHQVWWX	4	J	1	4			
Additional winning rack/draw combo = 28/10296 (SOUL wins 92/10296 altogether)							

SOUL's other 17 final margins are squeezed into the far right column of the (previous) SOU chart, where the sequences are identical except SOUL is played instead of SOU. All your final SOUL margins are *3 points lower*. (Without L hooking, SOUL + ULU scores less than SOU + ULU.) Most notably, in the M-rack scenario, played out in the **right-hand** diagram above, SOU wins by 1074, whereas SOUL critically wins the game by only 1071.

The number of possible ways to win may seem dizzying, but there is a lot of transposition. For you to win, Zoey must end up with one of only five different racks on her *second* turn (after playing EW and drawing a tile). She always acquires GJQVWX plus G, M, V, H or O, against which SOUL attains a final margin of 1094, 1071, 1046, 1038 or 270, respectively. SOU gets 3 points extra, but it loses (to SOUGH) in five of the seven H-rack scenarios.

We can quantify in equity dollars the difference between the two plays. With an extra 28 units (the second chart subtotal), SOUL (but not SOU) wins the game, for a gain of $2000. Offsetting that (see the M-rack sequence), with 32 units SOU (but not SOUL) ties for 2nd prize (instead of settling for 3rd); you nab an extra $1500. As 28 x $2000 is greater than 32 x $1500, SOUL has a higher equity than SOU (by the slight edge of $8000 divided by 10296).

In terms of just winning the *game* (ignoring chances to win higher tournament prizes), SOUL is easily better than SOU (by 92 units to 64 units), and *any* legal play you can make other than SOUL or SOU pales by comparison.

Going for the Gold

Some experts noted the merits of SOU and SOUL, though in the lexicon used in 1990 (OSPD-1), ULU and EW were unacceptable words. The only chance to play the 15-letter word as a bingo was if Zoey held GJQVVWW and you drew the X immediately (so as to shed your second and third U via LUX and XU). As a consequence, you were much less likely to win the game by a four-digit margin, and some variations involved struggling with two-U racks and needing specific tile-picking orders just to play OVEREMPHASIZING in two or three stages.

In this modern version of the puzzle (with ULU good, and despite EW being good), SOU and SOUL give you more ways not only to win the game (for third place) but also more ways to share second/third or win second prize.

From the standpoint of equity, it is possible to aim *even higher* with this four-step plan:

1. "Freeze" Zoey's rack: block all legal moves she can make if she holds **GJQVWWX**.
2. Play off all your other initial tiles except the A in such a way that Zoey cannot make a play and draw a tile.
3. Accumulate the GHMOVZ tiles in the bag.
4. Bingo out with (3x3x3) OVEREMPHASIZING for 1436 points (plus twice Zoey's tile values).

How do you pull off step 1? The key is to *burn your blank!* This has two benefits:

- It blocks both the I4 and I7 squares, thereby preventing Zoey from playing a tile. (No *non*-blank play from your rack can achieve this.) Otherwise, the points that Zoey scores in one or two turns along with some reduction in rack penalty, combined with the A-column points elucidated in the second bullet point (below), will likely determine which of the top three prizes ($10,000, $6000 or $3000) you take home.

- You score higher with a *non*-blank tile on the A-column. The difference is substantial, because the score of each tile is multiplied by 27, plus extra for a premium square and/or hooking a cross word. Compared to the blank, the letter value is boosted as follows: O +30, V +112, M +81, H +120, A +28, Z +560 or G +60.

Blank-burning Plays

To start with, allow me to demonstrate that even a *clumsy* blank-burning play offers winning chances.

No move with the blank gives you any hope if Zoey is able to play a tile. To prevent that, you can place tiles on both squares adjacent to a vowel with I4 **LUSh** (6): see the **left-hand** "close up" diagram below. You are still in a quandary, though, because the two U's on your rack play nowhere on their own, and you cannot afford to combine them with your A or any of the letters that you draw (GHMOVZ)—you need *all seven* of them for the A-column. Meanwhile, the U's occupy valuable space on your rack; you have to operate around them.

Clarification: to succeed after LUSh, GHMOVZ must be in the bag, so that you can combine them with your A and play the coveted 15-letter word. You know that this has a non-trivial chance of success once Zoey has passed.

In order to win, the rest of the parlay you need is that neither G nor Z is the last tile in the bag (the odds being 2:1 in your favor.) Your best initial draw includes GZ (20%) so that you can play SIZING (155); this empties the bag, and with an accumulated rack of AMOVZ (+UU), you can play OVEREMPHASIZING as a (five-tile) triple-triple for 409 points. You're still stuck with unplayable U's, so the game gets passed out and you win by 273.

In the more likely event you do *not* draw GZ, you can start with OCARINAS (30) and if your next tile pairs GZ (otherwise you lose), you play SIZING (155), draw the last tile (H, M or V) and finally play OVERMPHASIZING as a 4-tile play—a simple triple for 169 points. After the game is passed out, you emerge with a 25-point victory.

LUSh yields no follow-up U play   **pUS + pUL is a blunder, allows XU**   **uPS+pUL safely rids a second U**

Fortunately, you don't have to occupy *both* I4 and I7. A three-tile play, either from I4 to I6, or from I5 to I7, suffices to block both squares. Given that, is there a sequence that allows you to shed *two* U's instead of one?

Yes, but care is required. For example, if you play I5 pUS and then 5I pUL, shown in the **center** diagram above, such exposure of a U lets Zoey beat you by playing the X (at the little blue "x") and drawing the last tile in the bag.

The careful way is shown in the **right-hand** diagram: I5 **UpS** (6) + 6I pUL (or I4 SUp + 6I pUL, which also works). There, the presence of a tile to the left of the little "x" protects you from being punished by XU.

After UpS + pUL, with only one U burdening your rack, you are guaranteed to win by either 278 or 290 points. If the O is in the bag, you play SIZING; otherwise, you play OCARINAS. Either way, you collect the last tile in the bag and play the other five or six tiles together onto the A-column. (You eat the U, and Zoey eats GJQVWWX.)

To achieve a meaningful leap in your winning margin, you need to shed the third U. The key is to get all seven tiles slated for the A-column on your rack *at the same time*, so that you can score a 27-times bingo, instead of a 9-times non-bingo. Moreover, you can go out and collect double- instead of single-value from Zoey's rack.

Suitable for this purpose is a word that you rarely see played: **SUS**—and there are four different (relevant) ways to play it! The first letter can start at either I4 or I5, and the blank can stand for either the first S or the second S.

In all four SUS cases, you can shed both the second and third U with SULU next turn. However, there are subtle differences between these four candidates, each one deserving its own mini-diagram (mini-1 through mini-4).

Mini-1

Mini-2

As before, let us assume that Zoey holds GJQVWWX, and (therefore) GHMOVZ is in the bag. Otherwise, no blank-burning play can deliver the giant win you crave.

Mini-diagram 1 (**above, left**): You get 3 points for **I5 SUs**, followed by another 8 points for SULU (on a double-word score). After these two plays, you have shed *all three* U's, unburdening your rack.

Wait! Zoey gets to make a play (JUG)—isn't that verboten? No. You still win because you already played your sixth tile: you *emptied the bag*. In the previous central diagram (pUS + pUL), you play only *five* tiles; there, Zoey (plays XU and) draws the last tile in the bag and you fail to acquire all the letters you need for the A-column.

After JUG, you play the 15-letter word, stick Zoey with QVWWX, and win the game by 1150 points. Suddenly, you leapfrog over Xavier and *tie for first place*. This is a much better result than third place after UpS + pUL!

Mini-2 (**above**, **right**) and mini-3 (**below, left**): You score 2 fewer points for **I4 sUS** + SULU or **I4 SUs** + sULU than those two words score in mini-1. On the other hand, Zoey's JUG scores 11 fewer points (it misses the double-word score) in mini-2 and mini-3; instead of tying for first place, you win *sole* first place. Step aside, Will!

Mini-4 (below, right): As with mini-2, JUG hits you for 11 extra points (22 instead of 11.) However, sUS + SULU scores 12 points, which is 1 more than in mini-1. You win by 1151—just enough to slip you into sole first place!

So, mini-4 captures first place by only 1 point, compared to the 9-point margin attained in mini 2 or mini-3. That difference, though, is immaterial; $10,000 is won with all three choices. (Only mini-1's tie cashes less: $8000.) That stated, due to another aspect yet to be revealed, *all four* SUS options yield a different equity. Read on.

Mini-3

Mini-4

eXiGent circumstances

The unseen pool is GGHJMOQVVWWXZ. For you to burn the blank and have any chances to win, the H or M (playable near I13) cannot be on Zoey's rack. Nor can she have the Z or second G, because at a minimum, you need to play SIZING. You must assume she has a frozen rack of **GJQVVWWX minus one** tile (six possibilities).

For a crisper explanation, I describe these racks as –G, –J, –Q, –V, –W and –X. The correlating bag content is GHMOZ +1, described as +G, +J, +Q, +V, +W and +X. Example 1: if Zoey's frozen rack is –J (i.e., GQVVWWX), the bag is **+J** (i.e., GHJMOZ). Example 2: if her frozen rack is –V (the "main rack"), the bag is **+V** (the main bag), when you are poised to draw the perfect six tiles and you can win not only the game but also the whole tournament.

Remarkably, with a **+X** bag, you still win the game after any of the four initial SUS plays. If the X is in your initial draw (a 50% chance), you nimbly switch (from the now hopeless SULU or sULU) to the sequence in the **left-hand** diagram **below**. If your placement is I5, you win by 11 points with sUS or by 10 with SUs). If your SUS is *a line higher* (mini-2 or mini-3), instead play J6 HUM (creating 6I SH or sH) with your last three tiles, for a 3-point win.

Another revelation: I5 sUS (in mini-4) also wins with **+G**. If you immediately draw two G's (a 20% chance)—i.e., GGH, GGM, GGO or GGZ—you abandon sULU and play the sequence in the **right-hand** diagram **below** and win by 3 points! The first two SUS options (from mini-1 and mini-2) fall just short because their SUS + MO (or MOs) combinations each score 4 points less, ending in a 1-point loss. I4 SUs (from mini-3) + MO salvages a tie.

In the SUS chart beneath the diagrams below, the mini-diagram plays are listed in the order in which they appear, which is also in ascending order of equity. All three sources of frozen-rack equity, where applicable, are included.
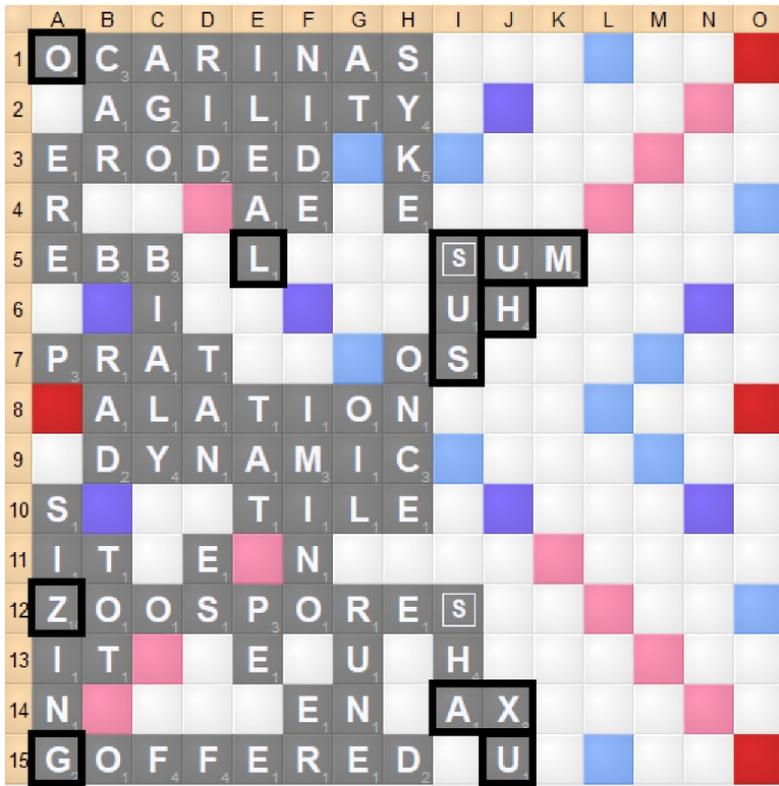
**Mini-4: the X appears immediately: I5 sUS +
ILEAL + AX + XU + OCARINAS + SIZING + SUM + UH = +11**

**Mini-4: two G's appear immediately: I5 sUS +
HUG + LUG + AH + OCARINAS + SIZING + MOS = +3**

Mini-diagram	Play	Bag	RackPr /1716	Adj	Prob /10296	Prize	$ Prize	Equity over $1000 ($ gain over 4th / 10296)	Total Gain /10296	Games /10296
Mini-1	I5 SUs	+V	4		24	1st =	8000	24 x 7000 = 168,000	I5 SUs 180,000	30
		+X	2	50%	6	3rd	3000	6 x 2000 = 12,000		
Mini-2	I4 sUS	+V	4		24	1st	10000	24 x 9000 = 216,000	I4 sUS 228,000	30
		+X	2	50%	6	3rd	3000	6 x 2000 = 12,000		
Mini-3	I4 SUs	+V	4		24	1st	10000	24 x 9000 = 216,000	I4 SUs 230,400	31.2
		+X	2	50%	6	3rd	3000	6 x 2000 = 12,000		
		+G	2	20%	2.4	3rd =	2000	2.4 x 1000 = 2,400		
Mini-4	I5 sUS	+V	4		24	1st	10000	24 x 9000 = 216,000	I5 sUS 232,800	32.4
		+X	2	50%	6	3rd	3000	6 x 2000 = 12,000		
		+G	2	20%	2.4	3rd	3000	2.4 x 2000 = 4,800		

Several other plays achieve results similar to I5 sUS (the last and best candidate in the above chart). We'll start with I5 **mUS** and I5 **nUS**, played in the same spot for the same score (6 points).

I5 mUS + ULU, MUX, OV- = +1157

I5 nUS + ULU, NUG, OV- = +1181

Having designated the blank an M or N (instead of S), you can't follow with sULU. However, you can instead shed your U's with J3 ULU (see diagrams **above**). After emptying the bag, you still have to tolerate Zoey playing a tile (with MUx or NUg), but after bingoing out you win the game by 1157 or 1181 (respectively), securing first place.

I4 SUm and **I4 SUn** (4 points) is a sort of inverse to the previous pair: the S is played next to the other vowel and the words are relatively spelled upside-down. The pair of follow-ups (see **below**) is thematically the same.

I4 **SUm** + ULU, MUX, OV- = +1168

I4 **SUn** + ULU, NUG, OV- = +1186

With +X and +G bags, I5 mUS or nUS are able to win, and by bigger margins than against I5 sUS, because the blank-M or -N can be hooked with a U (the blank-S cannot), allowing J5 UH for a good score. (Refer to the index in the extended version of the article linked at the end.) I4 SUm manages a small win not only with +X (see **below**) but also with +G (unlike the I4 SUS's in mini-2 and mini-3) because a U can be dumped to the right of the blank.

I4 SUn can also win with +G, but it stumbles into a catch-22 with the +X bag. The parallel sequence with I4 SUm is shown in the diagram **below**, where UH is your out-play and you win by 1 point. The catch is this: when the blank is changed from M to N, you cannot play MO before UH due to SUnG/MOG. It's a heartbreaker, but the best you can do is play UH first and let Zoey play 6I nUG (3); then you go out with MO and lose by 6.

That SUn conflict does not manifest with +G, because Zoey has no G to play. Without the risk of SUN/g or nU/G, I4 SUn therefore wins by the same 5-point margin that I4 SUm does with +G. Refer to the extended article.

**The X appears immediately: I4 sUM + AX + XU +
ILEAL + OCARINAS + SIZING + MO + UH(last) = +1**

Beware I4 nUS at I4; Zoey plays En/G and draws a tile. However, **I4 mUS** at I4 works—and more smoothly than I4 sUS. This clever 3-point play is the *only* way to prevent Zoey from playing a tile *after* you shed your third U.

As shown in the **left-hand** diagram **below**, your follow-up is J3 ULU (5), hooking Em/U. The upshot of this invulnerable placement is that you are able to win the game by 1191 and cinch first place by 41 points, leaving Will in the dust. The extra points are not worth any extra money (all finishing margins above 1150 pay the same), but you *can* boast that you snagged the highest winning margin that is attainable in the position.
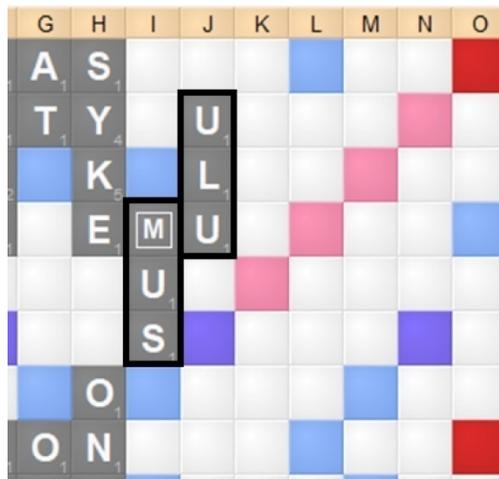
I4 mUS + ULU + OV- = +1191
(highest winning margin)

Two G's appear immediately: I4 mUS +
ILEAL+MO+OC-+SIZ-+HUG+AmUS+EmU= +4

I4 mUS also wins with +X and +G bags. With +X, apply the I4 SUm solution, except replace UH with SH + EmU (wins by 5). With +G, you can pull off a tricky 4-point win with a sequence involving the front-hook of A/mUS followed by the back hook of Em/U (a key U dump), as shown in the **right-hand** diagram **above**.

All the candidate plays we've examined up to this point that burn the blank also burn the typically valuable S. Instead, it is possible to save the S and initially play off the L. Resourcefulness is required, though, because without the L you are then unable to harness either of the convenient two-U-dump words SULU and ULU.

If you play **LUn** at **I5**, the trick to shucking two more U's is to extend On to OnUS (see **left-hand** diagram **below**). If you play **LUn** or **LUm** at **I4**, you similarly play nUS (or mUS) on the **right**. Either way, your follow-up is to play your last U (atop the S) with K5 US (which empties the bag). After Zoey plays JUS, you go out with your super-longo and win the game by 1153 or 1167, thereby procuring first place in the tournament.

I5 **LUn** + ONUS + US, JUS, OV- = +1153

I4 **LUn** + nUS (or **LUm** + mUS) + US, JUS, OV- = +1167
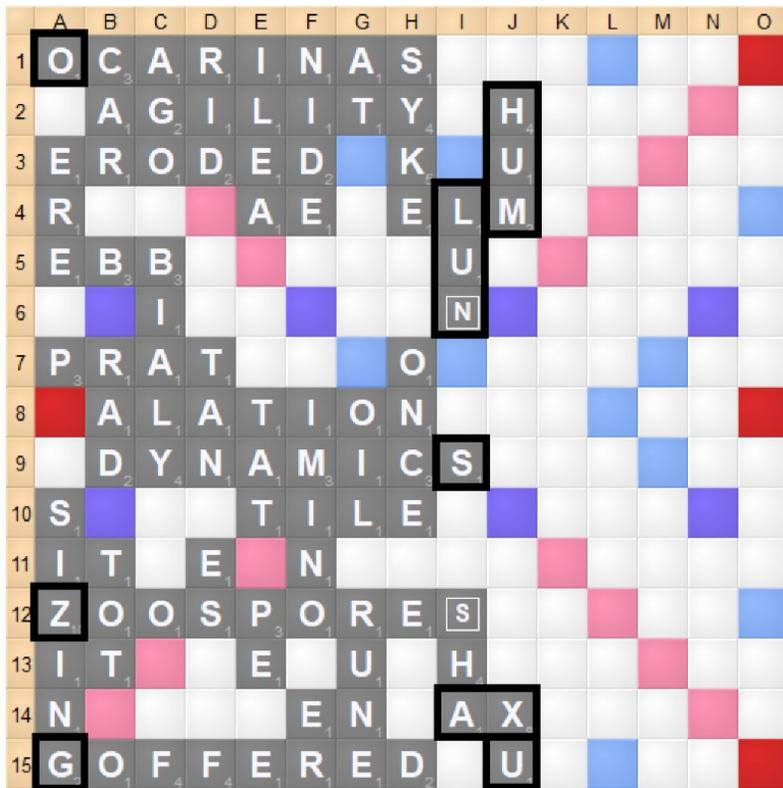
X appears in the initial draw: **I4 LUn** + DYNAMICS + AX + XU + OCARINAS + SIZING + HUM = +3

Two G's appear in the initial draw: **I5 LUn** + HUG + AH + OCARINAS + SIZING + MOn + US (last) = +3

As indicated (in the small diagrams on the previous page), playing I4 LUn, I4 LUm or I5 LUm can win the whole tournament with the main +V bag (V for Victory). In addition, you can win the game with the +X bag. For I4 LUn, though, you run into the same out-play conundrum that you do with I4 SUn, due to a LUNg collapse. Still, you can win anyway, thanks to the EL/M hook (which ES doesn't grant). See the **left-hand** diagram **above**.

You can also win with +G. If your initial move is LUn at I5, you win by dumping the third U with US/HUGS, as shown in the **right-hand** diagram **above**. This is a pivotal distinction between LUn and SUs. With SUs (or other S-U-blank word) at I5, you're stuck with the tiles LU (instead of SU), when LUG scores 4 points fewer than US.

Juicing the J

Amazingly, if you have played LUn or LUm at the higher I4 placement, you can save the game with yet another bag: **+J**. If the J is one of the three tiles in your initial draw (a 50% chance), you can switch to J3 US (!), which sets up a big J-spot that only you can exploit. With the sequence captioned under the **left-hand** diagram **below**, you eke out a tie. (OC- and SIZ- are abbreviations for OCARINAS and SIZING, played on the A-column.)

J appears immediately: **LUn/LUm/LUx** + US + JAM + AH + UM + OC- + SIZ- = tie

LUx + **xU** + US + JAM + OC- + SIZ- + **HM** (instead of AH + UM), you **lose by 1**

LUx + xU + US, JUS, OV- = +1151, (barely) first place

That brings us to the exquisite I4 **LUx**. With the desired +V bag, your winning follow-up is xU and J3 US (in that order), as shown in the **right-hand** diagram **above**. Zoey plays JUS (26), and you go out with the 1436-point bingo. The result is a 1151-point win, which earns you a final accumulative spread of +2151. This is only 1 point more than Will's spread, but it's all you need to take top honors in the tournament. Therefore, taking into account all the elements covered so far, I4 LUn, LUm and LUx at I4 (equally) share best-play status.

The coup de grâce is that in two bag situations (+G and +X), LUx has a subtle advantage over LUn or LUm:

As indicated (in the right-hand diagram above), after LUx your plan to win with **+V** is to play 6I xU next turn. You can efficiently do the same with **+X** and **+G**: your xU can be part of a winning sequence with *all three bags*. In other words, after LUx, if the key tile (the X or second G) is the fourth tile drawn, you can *still* win the game!

In both of the diagrams **below**, the same words are played after I4 LUx as after LUm, except mU at 6I has to be the out-play (or part of the UH out-play)—so as to dodge mU/X, whereas xU does not.

On the fourth tile, your chance of drawing the X is an extra 1/6, and your chance of drawing the second G is an extra 20%. This fourth-tile subtlety for +X and +G elevates I4 LUx above the second-best play of I4 LUn or LUm.

If xU + J3 US is part of your +V strategy, don't you get a free look at the fourth, fifth and sixth tile to see it is the J? No. Committing a U to 6J costs you a vital point; see the **central** diagram above. You can tie with +J only if you go directly from LUx to US, which would be a blunder (with a big +V win still possible) unless you draw the J right away. Therefore, achieving a tie with +J occurs no more often with LUx than with LUn or LUm in the same spot.
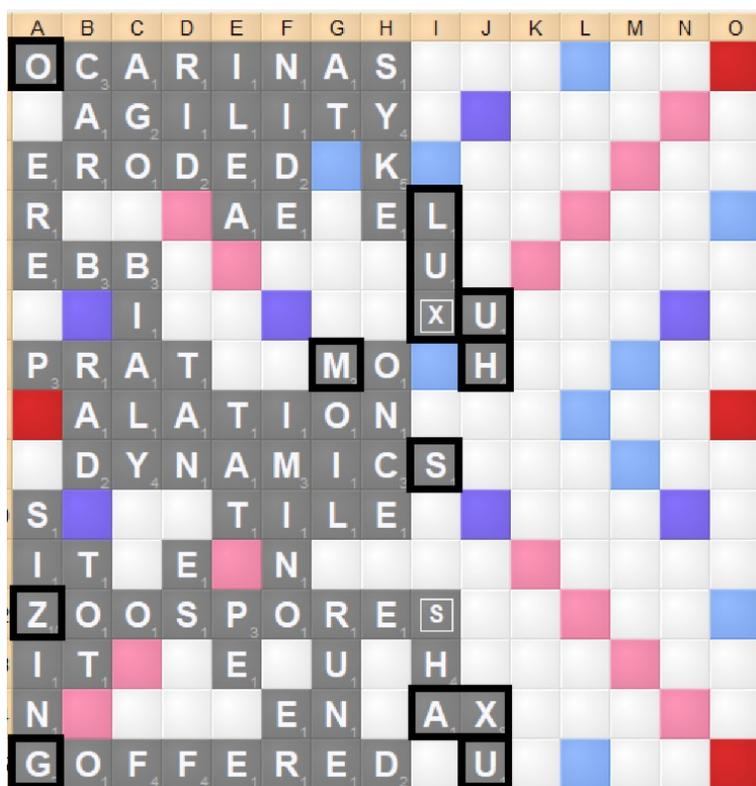
The X is the *fourth* tile drawn: LUx + xU +
DYNAMICS + AX + XU + OC- + SIZ- + MO + UH = +6

The G is the *fourth* tile drawn: LUx + xU +
DYNAMICS + HUG + AH- + OC- + SIZ- + MO = +12

When you burn your blank and Zoey passes, you encounter six possible bag situations. With four of them, you can win or a tie the game with the candidate plays listed in the table below.

Blank-burners: Success with Various Bags	
Bag	Game-winning (or tying) candidate plays and percentage
+G	I4 LUx (40%). I4 LUm, I4 or I5 LUn, I4 or I5 mUS, I5 nUS, I5 sUS, I4 sUM, I4 sUN and I4 sUS (tie) are all 20%
+J	I4 LUx, I4 LUn and I4 LUm are all 50% ties
+Q	none
+V	All plays covered in this article plus many lower-equity plays
+W	none
+X	I4 LUx (2/3). I4 LUm, I4 or I5 LUn, I4 or I5 mUS, I5 nUS, I4 or I5 sUS, I4 or I5 SUs and I5 sUM are all 50%

For reference, the nearest-miss sequence I found for +Q is is illustrated in the **left-hand** diagram below. The nearest-miss sequence I found for +W is illustrated in the **right-hand** diagram below.

The Q appears immediately: **I5 LUn** +
DYNAMICS + OC- + SIZ- + UH + LUM + QUA = –4

The W appears immediately: **I4 LUm** or **LUn** +
OC- + SIZ- + MO + MOA +SH + WUSHU = –3

Wrap-up

The question posed at the outset of this article was "**What is your best play in this unusual situation**?"

The answer is I4 **LUx**. It wins the tournament 100% of the time with the +V bag, and supplementally it wins the game 2/3 of the time with +X, 40% of the time with +G, and it ties 50% of the time with +J. It is the extra +X and +G vigorish that narrowly separates I4 LUx from the second-best play of I4 LUn or LUm.

If the question is altered to "What play is most likely to win the game?" SOUL stands out; it wins more than twice as often as LUx, which is in distant third behind SOU. However, with the puzzle conditions as stated, several blank-burning plays, which are in close rivalry for the top equity spot, outrank SOUL. Below is a summary chart.

LUx has the highest $ Gain / 10296. To calculate (prize) equity, add the $1000.00 (fourth prize) you're guaranteed to win as a minimum at the start of the game. Your average prize money when playing LUx is $1024.05.

UNUSUAL Puzzle: Ranking of Plays		
Candidate	$ Gain /10296	Games / 10296
I4 LUx	247,600	39.8
I4 LUn or LUm	238,800	35.4
I4 SUm mUS, I5 mUS nUS sUS LUn	232,800	32.4
I4 SUs	230,400	31.2
I4 sUS	228,000	30
I4 SUn	220,800	26.4
SOUL	196,000	92
SOU	188,000	64
I5 SUs	180,000	30

This article ends with the detailed chart starting on the next page. The **extended version** of this article, which includes an illustrative Index of Positions, can be found at

http://timothychow.net/UnusualPuzzle_extended.pdf

An article on the classic 1990 version of this puzzle, *An UNUSUAL Problem*, can be found at

https://timothychow.net/UNUSUAL.pdf

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An article on the *Equilibrium Puzzle*, composed by Nick Ballard and Timothy Y. Chow, can be found at

https://timothychow.net/EquilibriumPuzzle_extended.pdf

Will Anderson made a video about that Equilibrium Puzzle. *The ZEDONKS Conundrum* can be viewed at

https://www.youtube.com/watch?v=a2L60xgqB8o

A more mathematically oriented version of the Equilibrium Puzzle, *Bluffing in Scrabble*, can be found at

https://timothychow.net/scrabble.pdf

UNUSUAL Puzzle: Detailed Play Ranking

Play	Rack	Bag	RackPr /1716	Draw	DrawPr /6	Adj	Prob /10296	Prize	$ Prize	Equity over $1000 ($ gain over 4th / 10296)	Total Gain /10296	Games /10296
I4 LUx	GJQVWWX	+V	4	pass	6		24	1st	10000	24 x 9000 = 216,000	**I4 LUx** 247,600	39.8
	GJQVVWW	+X	2	pass	6	2/3	8	3rd	3000	8 x 2000 = 16,000		
	JQVVWWX	+G	2	pass	6	40%	4.8	3rd	3000	4.8 x 2000 = 9,600		
	GQVVWWX	+J	2	pass	6	50%	6	3rd=	2000	6 x 1000 = 6,000		
I4 LUm or LUn	GJQVWWX	+V	4	pass	6		24	1st	10000	24 x 9000 = 216,000	**I4 LUn** **I4 LUm** 238,800	35.4
	GJQVVWW	+X	2	pass	6	50%	6	3rd	3000	6 x 2000 = 12,000		
	JQVVWWX	+G	2	pass	6	20%	2.4	3rd	3000	2.4 x 2000 = 4,800		
	GQVVWWX	+J	2	pass	6	50%	6	3rd=	2000	6 x 1000 = 6,000		
I5 LUn	GJQVWWX	+V	4	pass	6		24	1st	10000	24 x 9000 = 216,000	**I5 LUn** 232,800	32.4
	GJQVVWW	+X	2	pass	6	50%	6	3rd	3000	6 x 2000 = 12,000		
	JQVVWWX	+G	2	pass	6	20%	2.4	3rd	3000	2.4 x 2000 = 4,800		
I4 mUS	GJQVWWX	+V	4	pass	6		24	1st	10000	24 x 9000 = 216,000	**I4 mUS** 232,800	32.4
	GJQVVWW	+X	2	pass	6	50%	6	3rd	3000	6 x 2000 = 12,000		
	JQVVWWX	+G	2	pass	6	20%	2.4	3rd	3000	2.4 x 2000 = 4,800		
I5 mUS or nUS	GJQVWWX	+V	4	pass	6		24	1st	10000	24 x 9000 = 216,000	**I5 mUS** **I5 nUS** 232,800	32.4
	GJQVVWW	+X	2	pass	6	50%	6	3rd	3000	6 x 2000 = 12,000		
	JQVVWWX	+G	2	pass	6	20%	2.4	3rd	3000	2.4 x 2000 = 4,800		
I5 sUS	GJQVWWX	+V	4	pass	6		24	1st	10000	24 x 9000 = 216,000	**I5 sUS** 232,800	32.4
	GJQVVWW	+X	2	pass	6	50%	6	3rd	3000	6 x 2000 = 12,000		
	JQVVWWX	+G	2	pass	6	20%	2.4	3rd	3000	2.4 x 2000 = 4,800		
I4 SUm	GJQVWWX	+V	4	pass	6		24	1st	10000	24 x 9000 = 216,000	**I5 SUm** 232,800	32.4
	GJQVVWW	+X	2	pass	6	50%	6	3rd	3000	6 x 2000 = 12,000		
	JQVVWWX	+G	2	pass	6	20%	2.4	3rd	3000	2.4 x 2000 = 4,800		
I4 SUs	GJQVWWX	+V	4	pass	6		24	1st	10000	24 x 9000 = 216,000	**I4 SUs** 230,400	31.2
	GJQVVWW	+X	2	pass	6	50%	6	3rd	3000	6 x 2000 = 12,000		
	JQVVWWX	+G	2	pass	6	20%	2.4	3rd=	2000	2.4 x 1000 = 2,400		
I4 sUS	GJQVWWX	+V	4	pass	6		24	1st	10000	24 x 9000 = 216,000	**I4 sUS** 228,000	30
	GJQVVWW	+X	2	pass	6	50%	6	3rd	3000	6 x 2000 = 12,000		
I4 SUn	GJQVWWX	+V	4	pass	6		24	1st	10000	24 x 9000 = 216,000	**I5 SUn** 220,800	26.4
	GJQVVWW	+G	2	pass	6	20%	2.4	3rd	3000	2.4 x 2000 = 4,800		

SOUL	GJQVWWX	G	4	G	1		4	2nd	6000	4 x 5000 = 20,000	SOUL	
	GJQVWWX	M	4	M	1		4				196,000	92
	GJMQVWW	M	4	X	1		4					
	GJMQVWX	M	8	W	1		8					
	GJMQWWX	M	2	V	2		4					
	GJMVWWX	M	4	Q	1		4					
	GMQVWWX	M	4	J	1		4					
	JMQVWWX	M	2	G	2		4					
	GJQVWWX	V	4	V	1		4					
	GJQVVWW	V	2	X	1		2					
	GJQVVWX	V	4	W	1		4	3rd	3000	88 x 2000 = 176,000		
	GJVVWWX	V	2	Q	1		2					
	GQVVWWX	V	2	J	1		2					
	JQVVWWX	V	1	G	2		2					
	GHJQVWW	H	4	X	1		4					
	GHJQVWX	H	8	W	1		8					
	GHJQWWX	H	4	V	2		8					
	GHJVWWX	H	4	Q	1		4					
	GHQVWWX	H	4	J	1		4					
	GJQVWWX	H	4	H	1		4					
	HJQVWWX	H	2	G	2		4					
	GJQVWWX	O	4	O	1		4					

SOU	GJQVWWX	G	4	G	1		4	2nd	6000	4 x 5000 = 20,000	SOU	
	GJQVWWX	M	4	M	1		4				188,000	64
	GJMQVWW	M	4	X	1		4					
	GJMQVWX	M	8	W	1		8	2nd=	4500	32 x 3500 = 112,000		
	GJMQWWX	M	2	V	2		4					
	GJMVWWX	M	4	Q	1		4					
	GMQVWWX	M	4	J	1		4					
	JMQVWWX	M	2	G	2		4					

	GJQVWWX	V	4	V	1		4					
	GJQVVWW	V	2	X	1		2					
	GJQVVWX	V	4	W	1		4					
SOU	GJVVWWX	V	2	Q	1		2					
(cont.)	GQVVWWX	V	2	J	1		2	3rd	3000			
	JQVVWWX	V	1	G	2		2			28 x 2000 = 56,000		
	GJQVWWX	H	4	H	1		4					
	HJQVWWX	H	2	G	2		4					
	GJQVWWX	O	4	O	1		4					
I5	GJQVWWX	+V	4	pass	6		24	1st=	8000	24 x 7000 = 168,000	**I5 SUs**	30
SUs *	GJQVVWW	+X	2	pass	6	50%	6	3rd	3000	6 x 2000 = 12,000	180,000	

*For the final entry, I5 SUs, the following substitutions for the blank yield the same equity: SUe, SUk, SUm, SUn, SUp.

 Note: Column 3 has a +Bag designation for the blank-burning plays, but it denotes a rack/draw designation for SOUL and SOU.

Convenience diagram below

Unseen: **GGHJMOQVVWWXZ (13)**